

N-36

Calorimetry



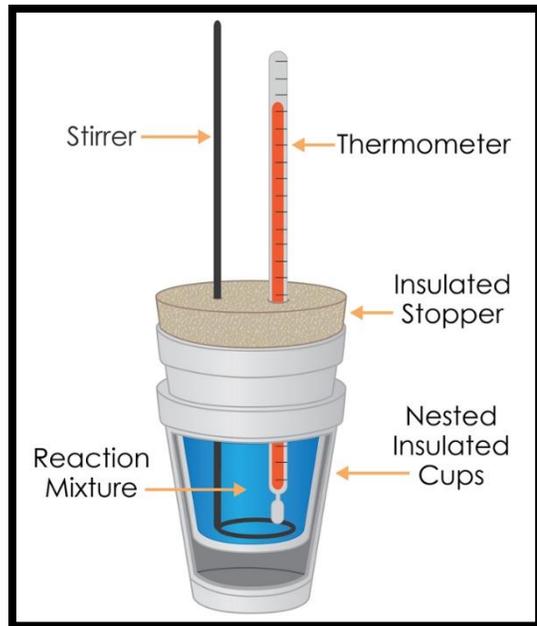
Target

I can use the 1st Law of Thermodynamics to solve “calorimetry problems” where I solve for information on one substance by knowing information on another substance.

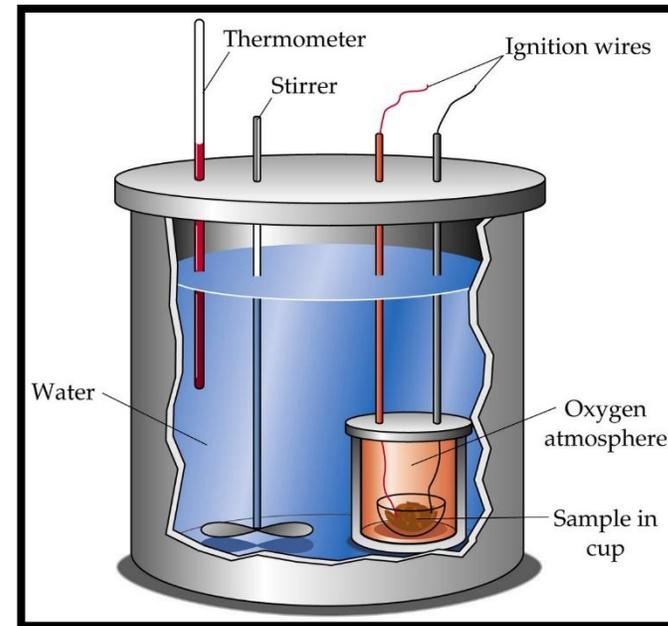
Purpose of Calorimetry

Measure heat transferred from one object to another, or the energy transferred during a reaction.

Coffee Cup Calorimeter



Bomb Calorimeter



Common Type of Question

- **Transferring a HOT object into a COLD liquid**
- **Transferring a COLD object into a HOT liquid**
- **Pouring two liquids together that start at different temperatures**
- **Calculating the heat released/absorbed during a chemical reaction**

Still Using

$$Q = mC\Delta T$$

These problems still involve energy

So we still use the $Q = mC\Delta T$ equation

BUT THIS TIME...

We need $Q = mC\Delta T$ for each substance...

We will have TWO $Q = mC\Delta T$ equations

How can we solve for a substance when we don't have enough information?

1st Law of Thermodynamics!

1st Law of Thermodynamics

Energy cannot be created or destroyed

We are TRANSFERRING energy

Therefore...

Energy In = Energy Out

Energy Absorbed = Energy Released

20 J of energy absorbed = 20 J of energy released

We need our math to match our concepts...

Energy In = Energy Out

Energy Absorbed = Energy Released

$$Q_{\text{substance 1}} = - Q_{\text{substance 2}}$$

Negative sign will stand for “OPPOSITE” not necessarily negative. Makes it so it doesn’t really matter which material you start with.

$Q = -Q$ shown with numbers

You put a hot piece of metal into a cold cup of water.

The water absorbs 50 Joules of energy, so the metal released 50 Joules of energy

$$Q_{\text{water}} = -Q_{\text{metal}}$$

endo *exo*

+ *-*

$$50 \text{ J} = -(-50 \text{ J})$$

Since our negative sign in our equation means opposite, the negatives will sort themselves out!

Think about where the negatives are coming from...

$m = \text{always } +$

$C = \text{always } +$

$\Delta T = + \text{ or } - \quad !!!$

Therefore...

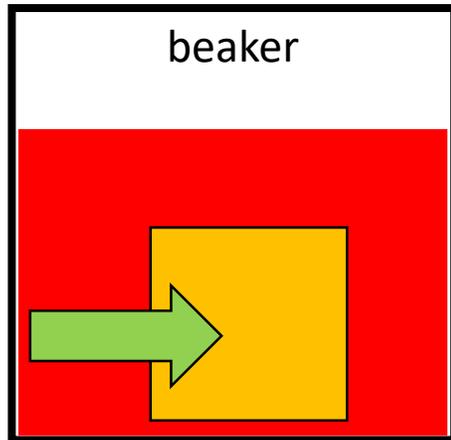
$Q \text{ can end up } + \text{ or } -$

Example with Pictures

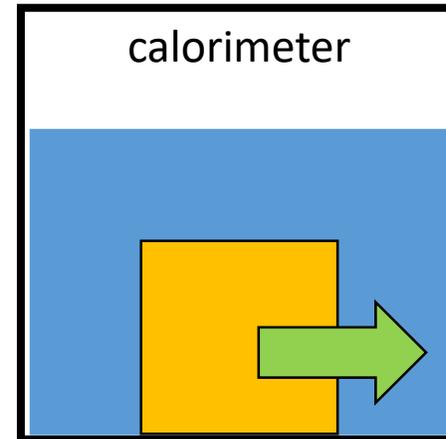
ENERGY IN = ENERGY OUT

Energy absorbed $\rightarrow Q = +$
Energy released $\rightarrow Q = -$

$$Q_{\text{metal}} = +$$
$$Q_{\text{water}} = -$$



Hot Water
Metal is heating up
Energy transfer into METAL



Cold Water
Water is heating up
Energy transfer into WATER

$$Q_{\text{metal}} = -$$
$$Q_{\text{water}} = +$$

Key Thing to Note About T_{final}

If you leave the object/liquid/solutions together long enough they will come to the same temperature!

Example:

$$T_{\text{final}}_{\text{water}} = T_{\text{final}}_{\text{metal}}$$

A very convenient fact that will simplify the algebra to allow us to solve for various things.

$$Q_{\text{water}} = \text{?}$$

$$m_{\text{water}} = \text{From the water you put in the calorimeter}$$

1mL = 1g

$$C_{\text{water}} = 4.184 \text{ J/g}^\circ\text{C}$$

$$\Delta T_{\text{water}} = T_f - T_i$$

(From your thermometer readings)

$$Q_{\text{metal}} = -Q_{\text{water}}$$

Energy IN must = energy OUT!
(opposite sign, not necessarily negative)

$$m_{\text{metal}} = \text{From your scale}$$

$$C_{\text{metal}} = \text{?}$$

$$\Delta T_{\text{metal}} = \begin{matrix} T_f - T_i \\ T_f - 100^\circ\text{C} \end{matrix}$$

(At the end the metal and water will be same temp) From water From boiling
(The metal was put in the boiling water so it reached 100°C)

Practice Problems

- **Glue the questions in your notebook**
- **Show your work the way I do!**
- **Annotate the practice problems with comments, tips, warnings, explanations, etc!**
These are NOTES not just practice problems!

Practice Problems

- 1) Calculate the specific heat of a metal if 2.36×10^2 grams of it at 99.5°C is added to 125.0 mL of water at 22.0°C . The final temperature of the system is 25.4°C .
- 2) A lump of chromium (Cr) has a mass of 95.3 grams and a temperature of 90.5°C . It is placed into a calorimeter with 75.2 mL of water at 20.5°C . After stirring, the final temperature of the water, Cr metal, and calorimeter is 28.6°C . What is the specific heat of Cr metal?
- 3) A 100.0 gram sample of water at 50.0°C is mixed with a 50.00 gram sample of water at 20.0°C . What is the final temperature of the 150.0 grams of water?

① metal

$$Q = -$$

$$m = 2.36 \times 10^2 \text{ g}$$

$$C = ?$$

$$\Delta T = T_f \quad 25.4^\circ\text{C}$$

$$-T_i \quad -99.5^\circ\text{C}$$

Cooling down -74.1°C

water

$$Q = -$$

$$m = 125 \text{ g}$$

$$C = 4.18 \text{ J/g}^\circ\text{C}$$

$$\Delta T = T_f \quad 25.4^\circ\text{C}$$

$$-T_i \quad -22^\circ\text{C}$$

heats up 3.4°C

$$Q = -Q$$

So we don't need the actual Q values!

← Known value, look it up!

Not given in the Question

$$Q = mC\Delta T$$

$$Q = -Q$$

\Rightarrow

$$mC\Delta T_{\text{Substance 1}} = -mC\Delta T_{\text{Substance 2}}$$

$$= -mC\Delta T_{\text{Substance 2}}$$

metal

doesn't matter which subst. is #1 or #2

water

$$(2.36 \times 10^2 \text{ g})(C)(-74.1^\circ\text{C}) = -(125 \text{ g})(4.18 \frac{\text{J}}{\text{g}^\circ\text{C}})(3.4^\circ\text{C})$$

Solve!

Careful about negative signs!

$$C = 0.102 \text{ J/g}^\circ\text{C}$$

metal

② Chromium

$$Q =$$

$$m = 95.3 \text{ g}$$

$$c = ?$$

$$\Delta T = T_f \quad 28.6^\circ\text{C}$$

$$- T_i \quad -90.5^\circ\text{C}$$

$$\text{cools down} \quad -61.9^\circ\text{C}$$

Water

$$Q =$$

$$m = 75.2 \text{ g}$$

$$c = 4.18 \frac{\text{J}}{\text{g}^\circ\text{C}}$$

$$\Delta T = T_f \quad 28.6^\circ\text{C}$$

$$- T_i \quad -20.5^\circ\text{C}$$

$$\text{heats up} \quad 8.1^\circ\text{C}$$

$$Q = -Q$$

$$mC\Delta T = -mC\Delta T$$

* Don't be sloppy,
with negatives!
they mean
something! they
matter!

Chromium

$$(95.3 \text{ g})(c)(-61.9^\circ\text{C}) = -(75.2 \text{ g})(4.18 \frac{\text{J}}{\text{g}^\circ\text{C}})(8.1^\circ\text{C})$$

c	$= 0.432 \frac{\text{J}}{\text{g}^\circ\text{C}}$
Chromium	

③ water #1

$$Q = \rightarrow$$

$$m = 100g$$

$$C = 4.18 \text{ J/g}^\circ\text{C}$$

$$\Delta T = T_f - T_i$$
$$= T_f - 50^\circ\text{C}$$

water #2

$$Q = -$$

$$m = 50g$$

$$C = 4.18 \text{ J/g}^\circ\text{C}$$

$$\Delta T = T_f - T_i$$
$$= T_f - 20^\circ\text{C}$$

$$Q = -Q$$

* Both substances
end at same
temp! Same
 T_{final} values!

water #1

$$(100g)(4.18 \text{ J/g}^\circ\text{C})(T_f - 50^\circ) = -(50g)(4.18 \text{ J/g}^\circ\text{C})(T_f - 20^\circ)$$

* don't be lazy! Show algebra steps to help!
So many lost points on calorimetry problems
because of algebra and calculator mistakes.

water #1

$$(100\text{g})(4.18\text{ J/g}^\circ\text{C})(T_f - 50^\circ\text{C}) = - \frac{\text{water \#2}}{(50\text{g})(4.18\text{ J/g}^\circ\text{C})(T_f - 20^\circ\text{C})}$$

* TIPS

distribute
everything then
combine variables
and then isolate

* still just solving
for missing
variable! just
more to
rearrange!

* careful to
distribute
negative signs
and with
double negatives

Algebra Steps for #3

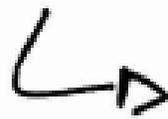
$$\begin{array}{r} 418 T_f - 20900 = -209 T_f + 4180 \\ + 209 T_f \qquad \qquad \qquad + 209 T_f \end{array}$$



$$\begin{array}{r} 627 T_f - 20900 = 4180 \\ + 20900 \qquad \qquad + 20900 \end{array}$$



$$\frac{627 T_f}{627} = \frac{25080}{627}$$



$$\boxed{T_f = 40^\circ\text{C}}$$